



**CHALMERS**

UNIVERSITY OF TECHNOLOGY

# **EFFICIENT (AND ROBUST) ANALYSIS OF PROGRESSIVE FAILURE IN FIBRE- REINFORCED POLYMERS**

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# AUTOMOTIVE ELECTRIFICATION



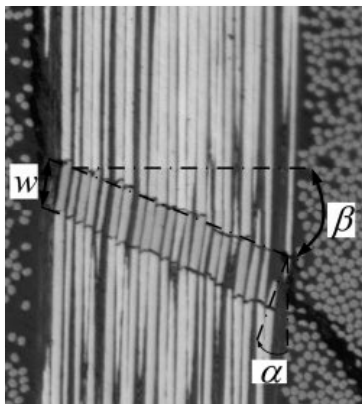
**SUSTAINABLE AVIATION**

# What is “failure”?

*“When and how a component or structure is deforming and eventually failing to fulfil its intended function”*



T.T. Ng, 2016



R. Gutkin, 2010

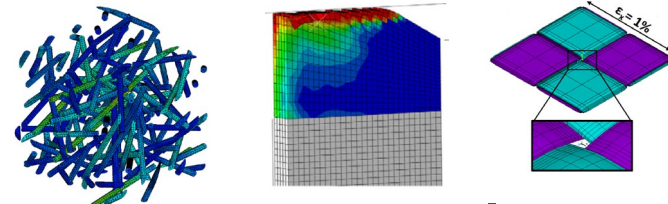


www.motor1.com

# There are challenges on all scales!

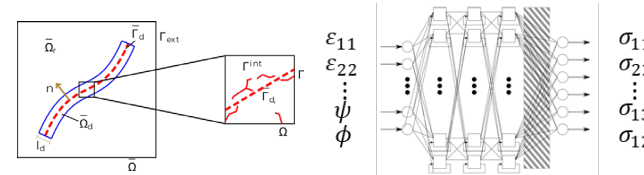
- How to properly model damage and fracture on the micro- or mesoscale?

- Sérgio Costa, Hana Zrida, Mohsen Mirkhalaf, ...



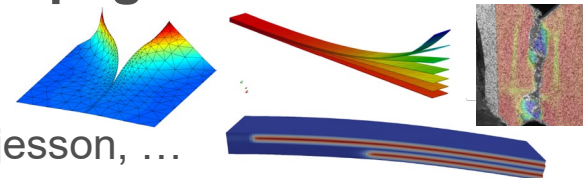
- How to efficiently link the microscale behaviour to macroscale performance?

- Erik Svenning, Mohsen Mirkhalaf, Ehsan Ghane, ...



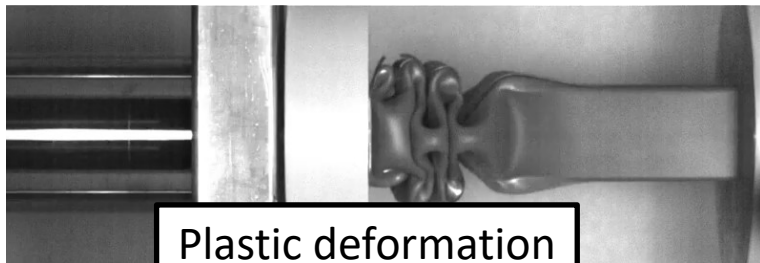
- How to efficiently model damage and crack propagation on the macroscale?

- Salar Mostofizadeh, Jim Brouzoulis, Johannes Främby, Pierre Daniels, Carolyn Oddy, Camiel Adams, Elias Börjesson, ...

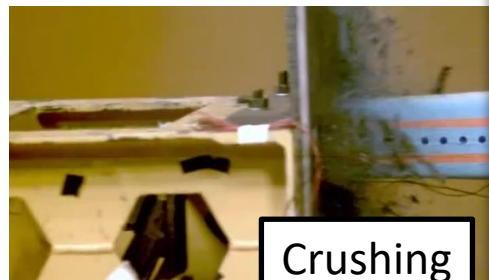


# Automotive crash simulations

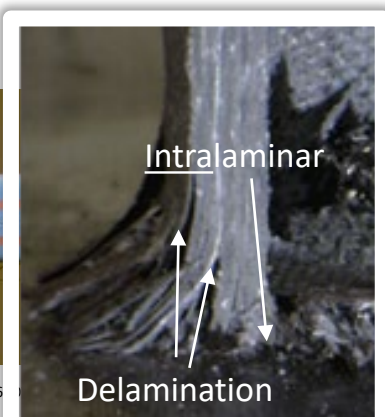
## METAL CRASH BOX



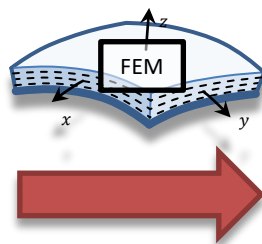
## COMPOSITE CRASH BOX



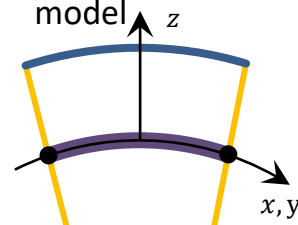
Courtesy of Engenuity: <https://www.youtube.com/watch?v=VdP5a4k6>



Grauers, Olsson & Gutkin (2014), *Compos Struct*



Single-layer model



Entire thickness represented by one shell element.

Computationally efficient

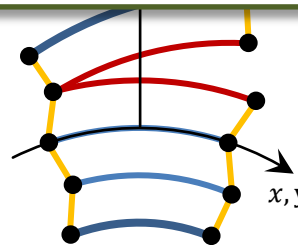
Not for composites  
(can't model delamination)

Research scope:

Develop **accurate** and **efficient** shell models for FE simulation of failure in composites

Each ply represented by separate element layer.

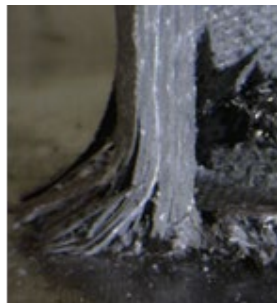
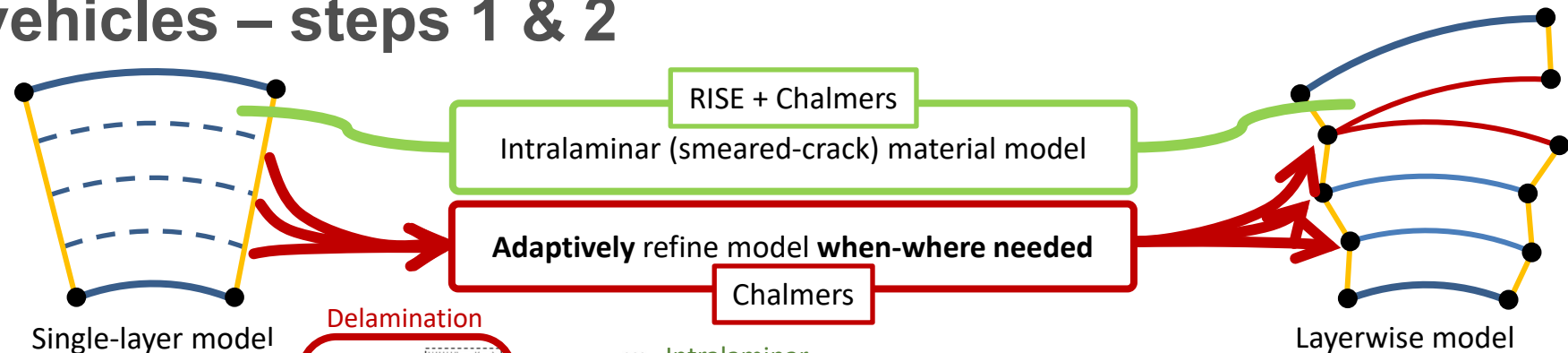
Interface modelled by cohesive elements



Accurate prediction  
(includes delaminations)

VERY computationally expensive

# Modelling of crash behaviour in future lightweight vehicles – steps 1 & 2



Grauers, Olsson & Gutkin (2014).  
*Compos Struct*

Intralaminar

Delamination

Delamination: mode I

Delamination: mixed mode

Kink band through part intralaminar of bundle shear cracking

Intralaminar

Matrix cracking

Kink bands and matrix cracking

Debris wedge

Grauers, Olsson & Gutkin (2014),  
*Compos Struct*

Bending failure

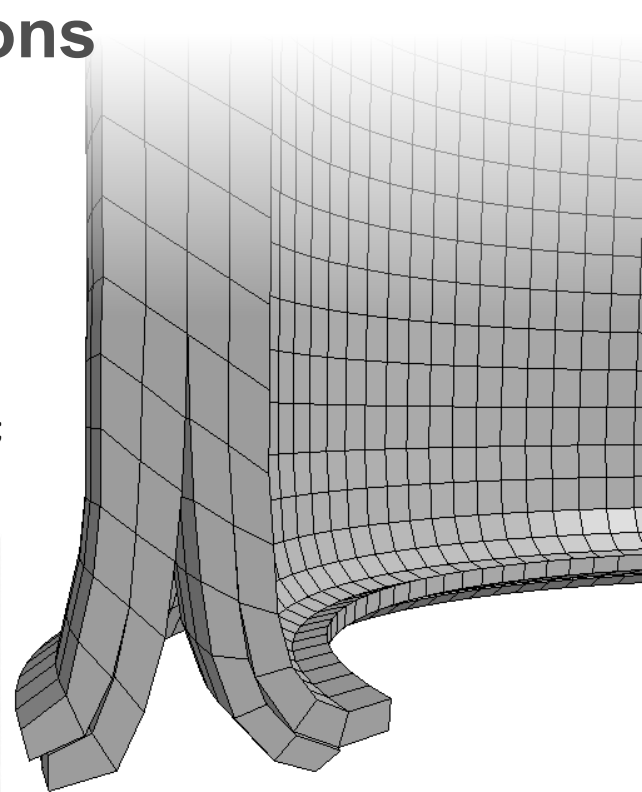
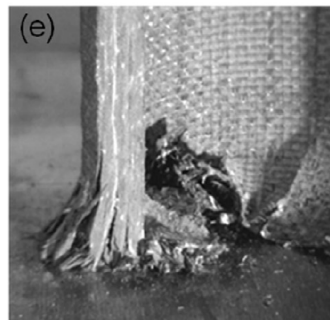
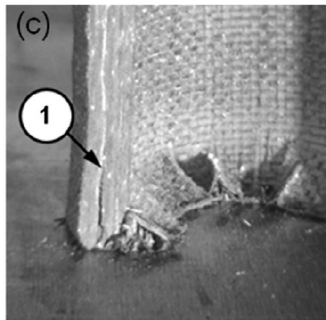
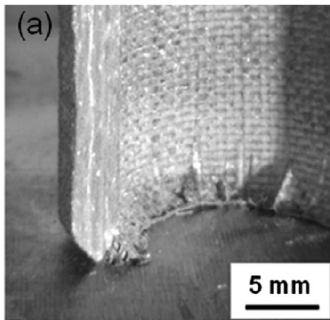
Compressive failure



# Adaptive method to model delaminations

Johannes Främby, Jim Brouzoulis, Jesper Karlsson & MF

1. Starts with one shell element through the thickness;
2. Identify potential refinement areas with refinement indicators;
3. Shell is locally refined through the thickness (weak refinement);
4. If necessary: cohesive interfaces introduced (strong refinement);
5. If delaminations propagate, refinements are expanded in plane.



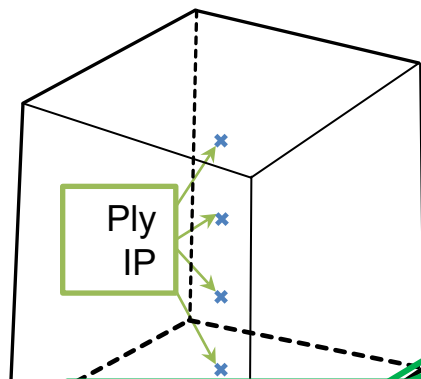
Adapted from: Grauers, Olsson & Gutkin (2014). *Composite Structures*

# Adaptive LS-DYNA thick shell element

Johannes Främby, Jim Brouzoulis, Jesper Karlsson & MF

## Unrefined element

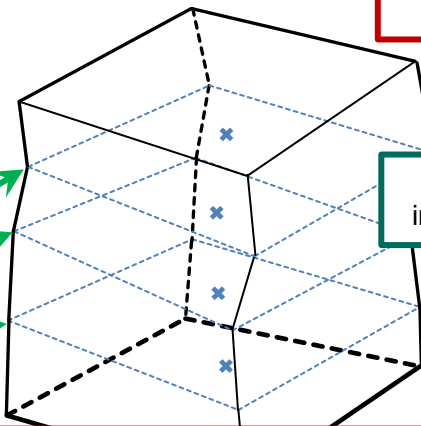
User element: 8 noded thick shell  
ELFORM 3 and 5



Element **divided** into subelements  
by assigning **global extra nodes** to  
represent the ply interfaces.

Augmented FEM – Ling et al (2009). *Int. J. Fract.*

## Weak refinements (increase resolution)

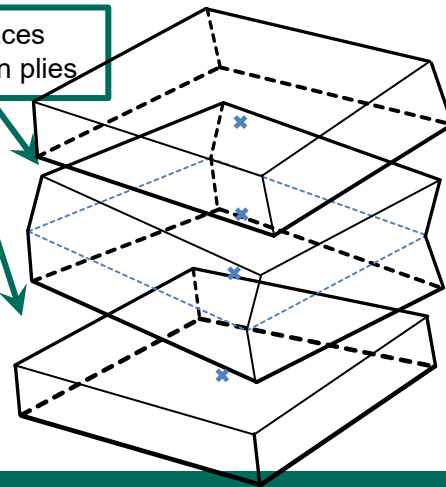


When subelements are  
introduced, the nodal masses  
are adjusted appropriately.

- No additional IP added, no IP-data mapping required.
- Refinement done during simulation. No restarts made.
- The time step is automatically updated. Also takes material orthotropy into account (allows for slender elements when  $E_3 < E_1$ )

## Strong refinements (model delaminations)

Cohesive interfaces  
introduced between plies



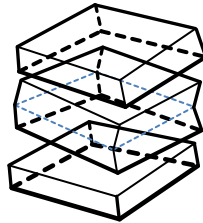
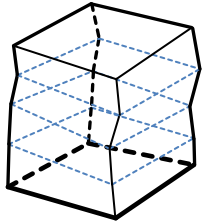
# Refinement indicators/damage initiation criteria

Johannes Främby, Pierre Daniel, Jim Brouzoulis & MF

## Weak refinements (increase resolution)

- Evaluate ply failure indices.
- Requires an educated guess of the refined stress state.
  - Stress recovery technique can assist.  
Främby et al (2017). *IJNME*. - flat  
Daniel et al. (2019), *Composite Structures* – doubly curved

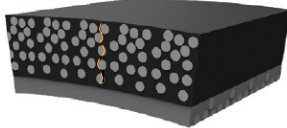
Refinements should be done before failure initiates!



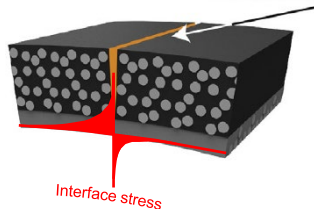
## Strong refinements (model delaminations)

- Evaluate delamination failure index.
- Monitor formation of intralaminar cracks.

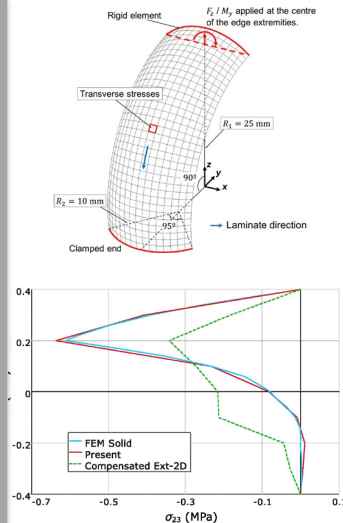
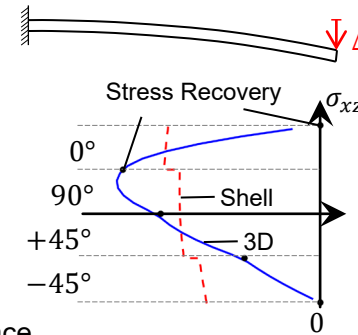
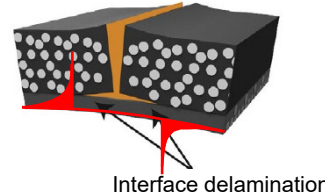
Transverse matrix crack initiated



Fully evolved matrix crack.

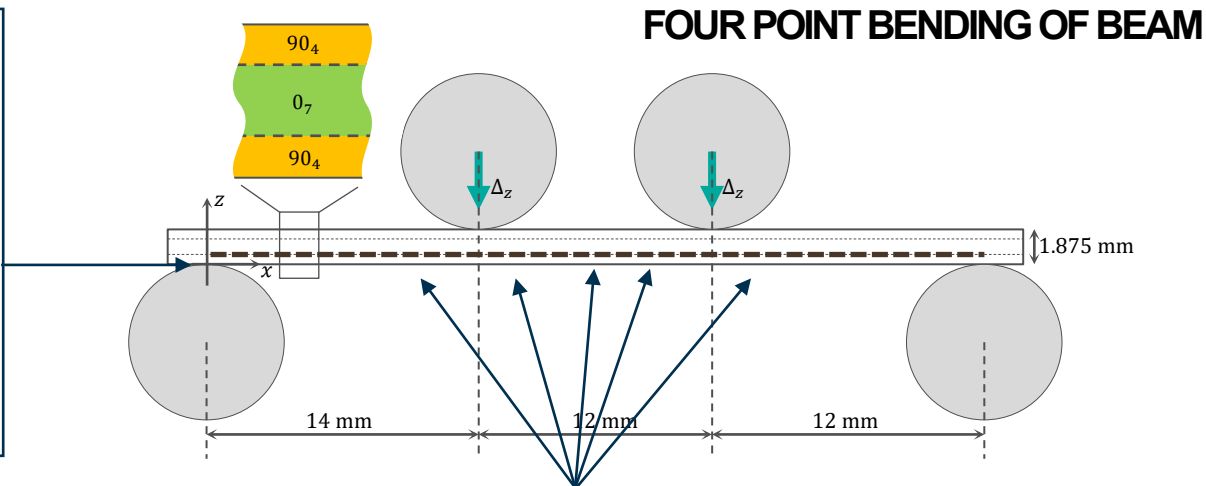
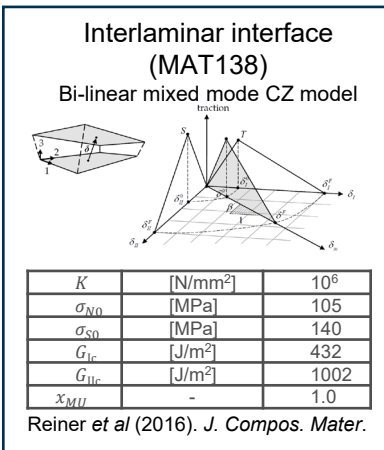


Interface delamination



# Matrix Crack Induced Delaminations

Främby and Fagerström, Engineering Fracture Mechanics, 2021



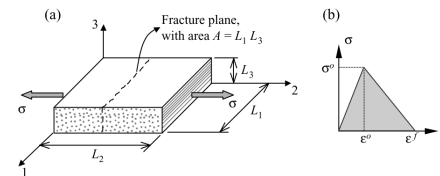
### Comparison to

- Reference model with explicit matrix crack;
- Experiment by Mortell *et al.*



Mortell *et al* (2014), *Compos. Sci. Technol.*

### Smeared intralaminar crack modelling



Pinho *et al* (2006). *Comp Part A.*

HTA/6376		
$E_1$	[GPa]	140
$E_2, E_3$	[GPa]	10
$G_{12}, G_{13}$	[GPa]	5.2
$G_{23}$	[GPa]	3.9
$\nu_{21}, \nu_{31}$	-	0.0214
$\nu_{32}$	-	0.5
$Y_T$	[MPa]	62
$G_{Ic,mt}$	[J/m <sup>2</sup> ]	432

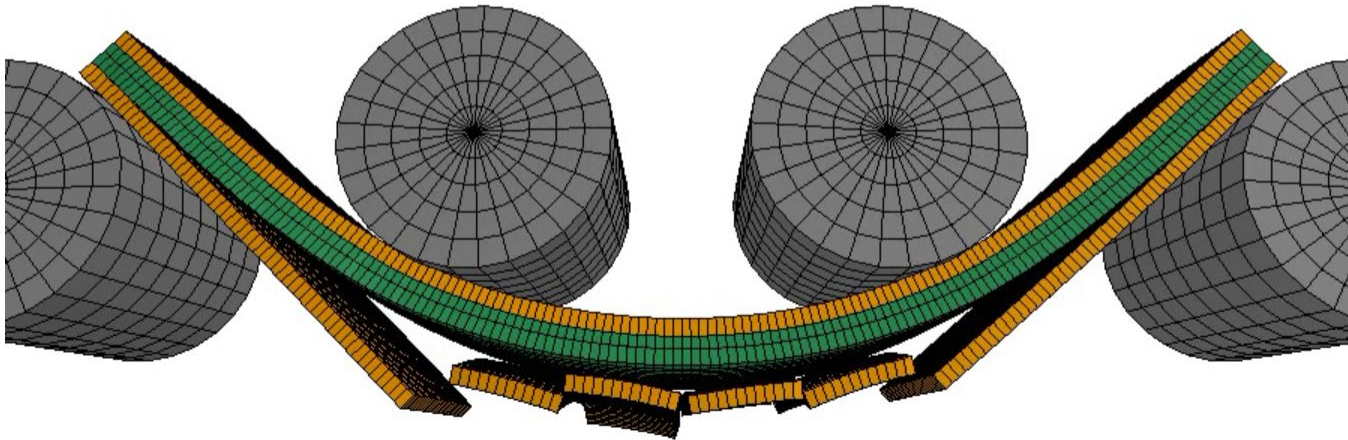
Reiner *et al* (2016). *J. Compos. Mater.*

# Matrix Crack Induced Delaminations

Främby and Fagerström, Engineering Fracture Mechanics, 2021

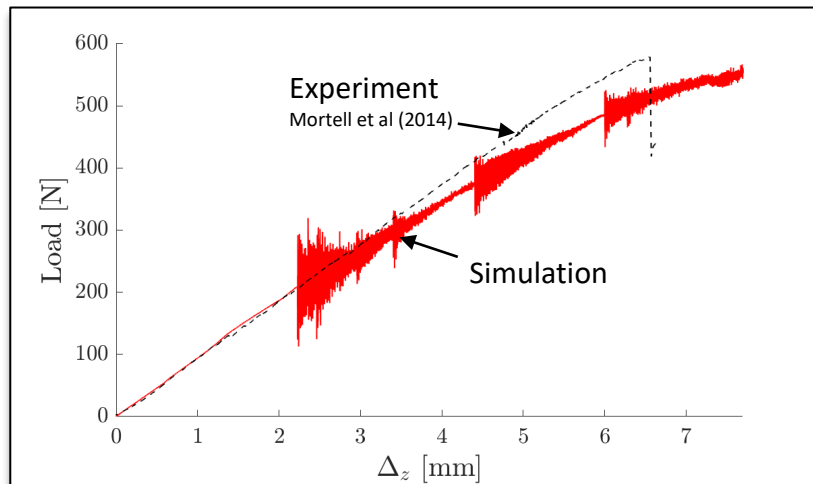
MCID 4PB ref usermat - units mm/ms/kg/(kN/GPa)

Time = 20.8



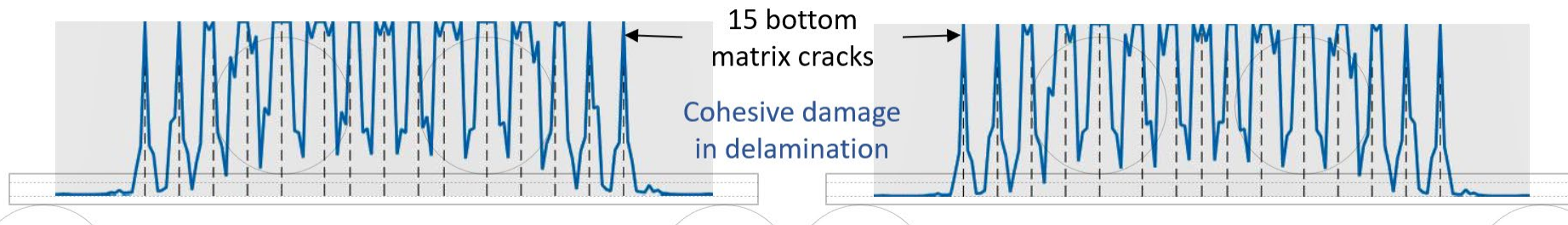
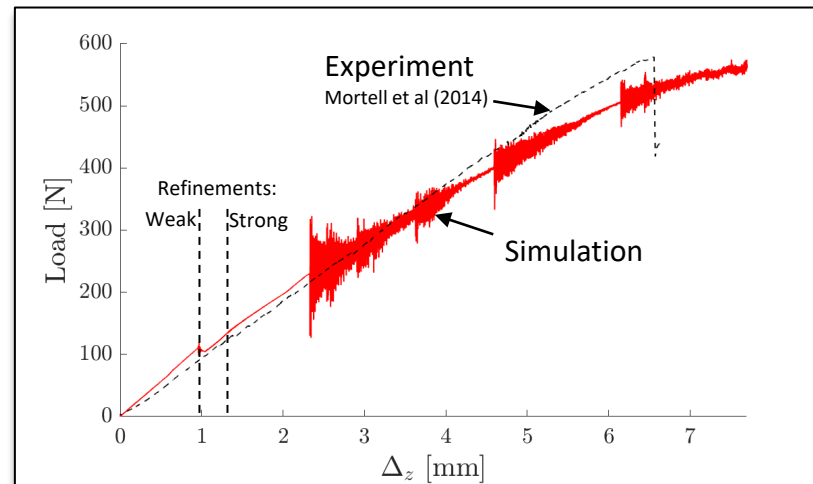
Reference model

## NON-ADAPTIVE REFERENCE



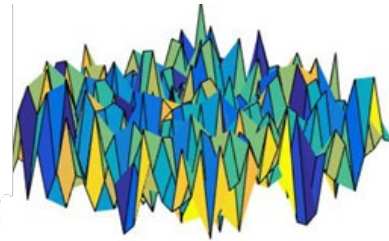
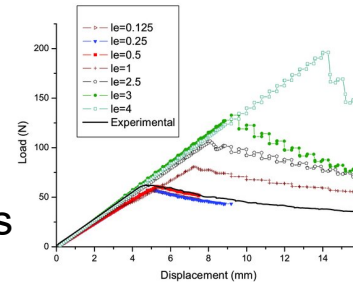
## ADAPTIVE

With stabilisation of weak refinement



# Efficient adaptive simulations of progressive failure

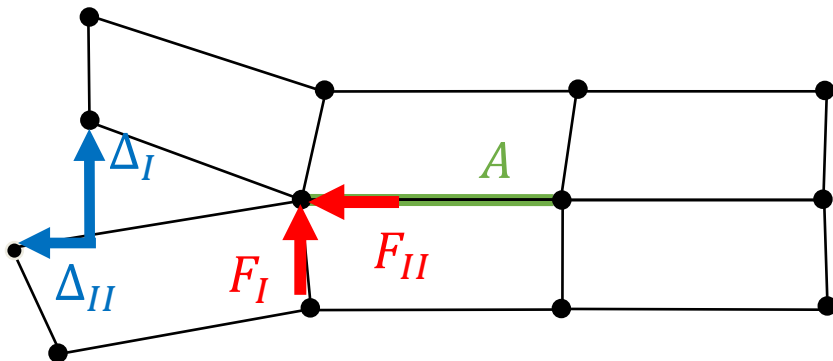
- Adaptive modelling of delamination growth can be achieved by adding additional degrees of freedom on the fly
  - Weak and strong discontinuities both have advantages
- An adaptive strategy requires suitable refinement indicators
  - Stress-based for initiations, damage-based for growth
- What remains:
  - The curse of cohesive zone modelling:  
Requires very small elements for brittle materials
  - Brittle failure requires robust solution methods



# Mitigating the requirement on small in-plane element size

Pierre Daniels, Johannes Främby, MF and Pere Maimí: *Under review*

## 1. Use VCCT as propagation criterion



$$G_I = \frac{F_I \langle \Delta_I \rangle}{2A}$$

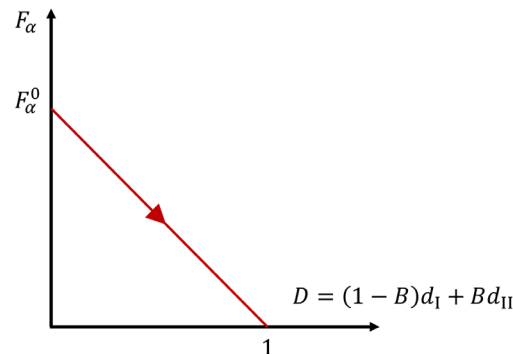
$$G_{II} = \frac{F_{II} \Delta_{II}}{2A}$$

$$G_T = G_I + G_{II}$$

If  $G_T > G_C$  **→** The crack has grown

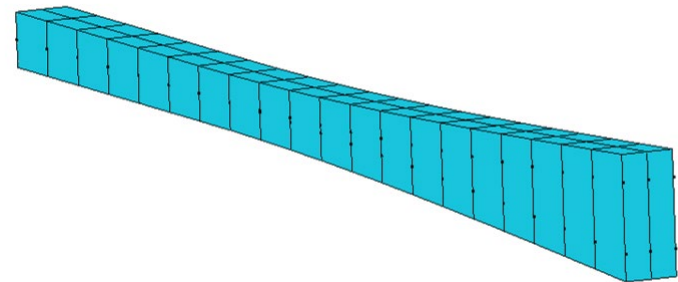
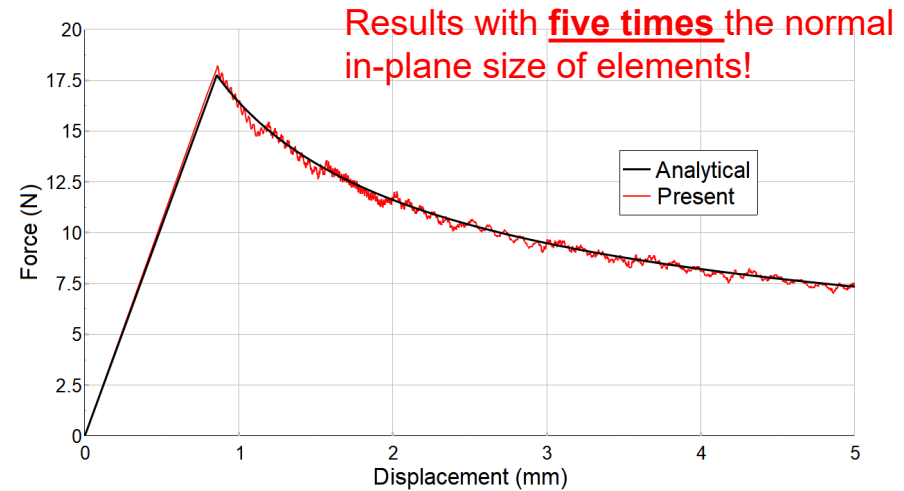
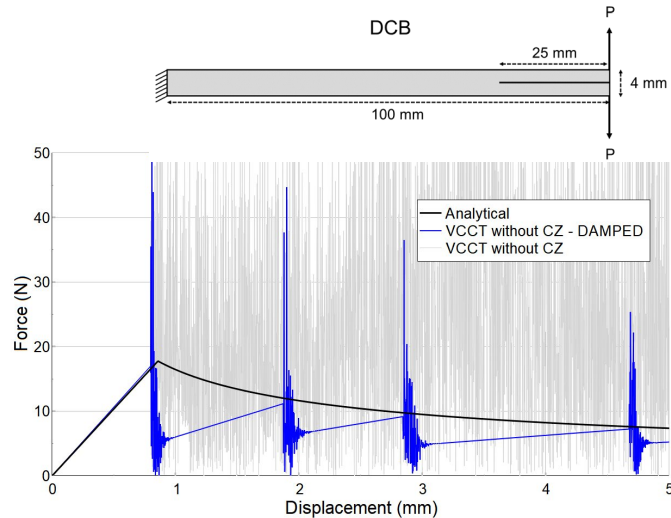
## 2. Use a cohesive zone like dissipative mechanism

$$F_\alpha = F_\alpha^0 (1 - D) \quad ; \quad (\alpha = I, II)$$



# Mitigating the requirement on small in-plane element size

Pierre Daniels, Johannes Främby, MF and Pere Maimí: *Under review*



# A novel dissipation-based path-following solver

Elias Börjesson, Joris Remmers and MF: *Computational Mechanics* 2022

- Adding an additional unknown load factor  $\lambda$  to the system

$$\mathbf{r}(\mathbf{a}, \lambda) = \mathbf{f}^{int}(\mathbf{a}) - \lambda \hat{\mathbf{f}} = 0$$

External reference nodal load vector

- Controlled by an additional equation  $\varphi$  constraining the total dissipation

$$\varphi(\mathbf{a}) = \int_{\Omega} \Delta D dV - \Delta L = 0$$

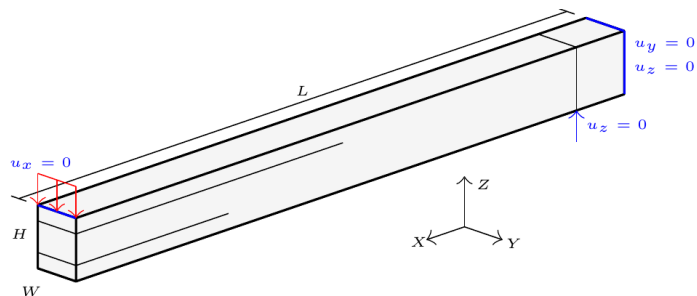
Max dissipation during a load step

- Almost too simple! But it works!

# Example - Multiple end loaded split

Elias Börjesson et al., Computers & Structures 2002

Note! Model is initially one shell through the thickness!



## Geometry:

$L = 110$  mm,  $W = 20$  mm,  $H = 8$  mm

Lower crack length: 32 mm

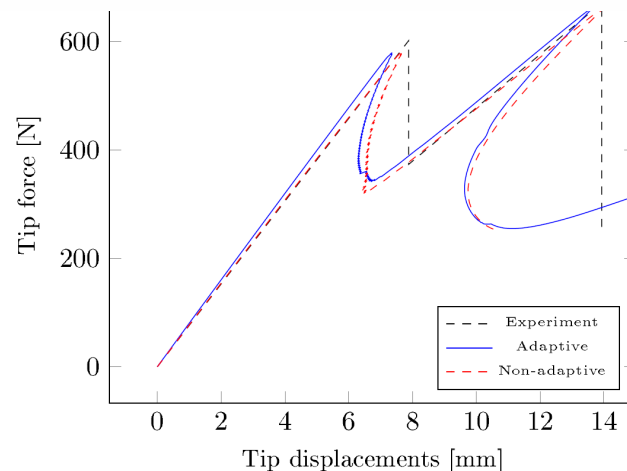
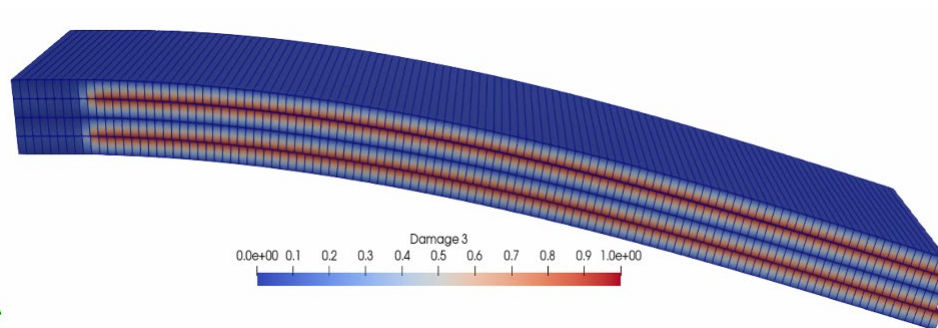
Upper crack length: 56 mm

## Material IM7/8552 carbon-epoxy:

Homogenized material properties

$$\begin{array}{lll} E_1 = E_2 = 61.65 \text{ GPa} & G_{12} = 23.37 \text{ GPa} & \nu_{12} = 0.3187 \\ E_3 = 13.61 \text{ GPa} & G_{13} = G_{23} = 4.55 \text{ GPa} & \nu_{13} = \nu_{23} = 0.3161 \end{array}$$

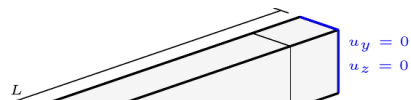
Experiment by Yasaei et al., 2016



# Example - Multiple end loaded split

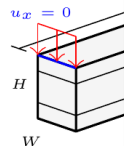
Elias Börjesson et al., Computers & Structures 2002

Note! Model is initially one shell through the thickness!



Element configuration

Interface damage



Geomet

$L = 110$

Lower c

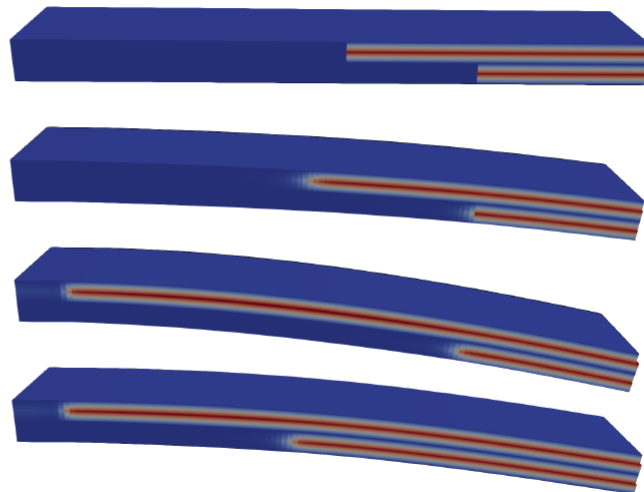
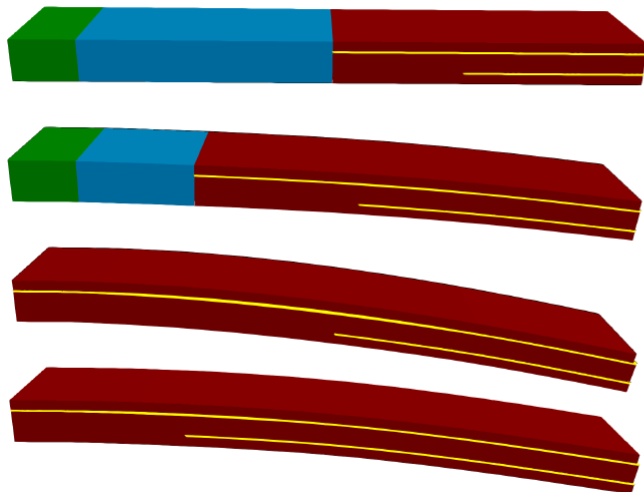
Upper c

Material

Homoge

$E_1 = E_2 = 6$

$E_3 = 13.61$



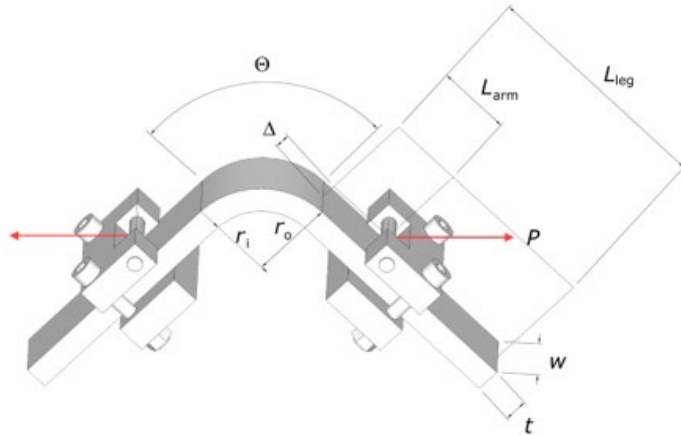
0 2 4 6 8 10 12 14

Tip displacements [mm]

Experiment by Yasaei et al., 2016

# Example - “NASA specimen”

Elias Börjesson, Joris Remmers and MF: *Computational Mechanics 2022*

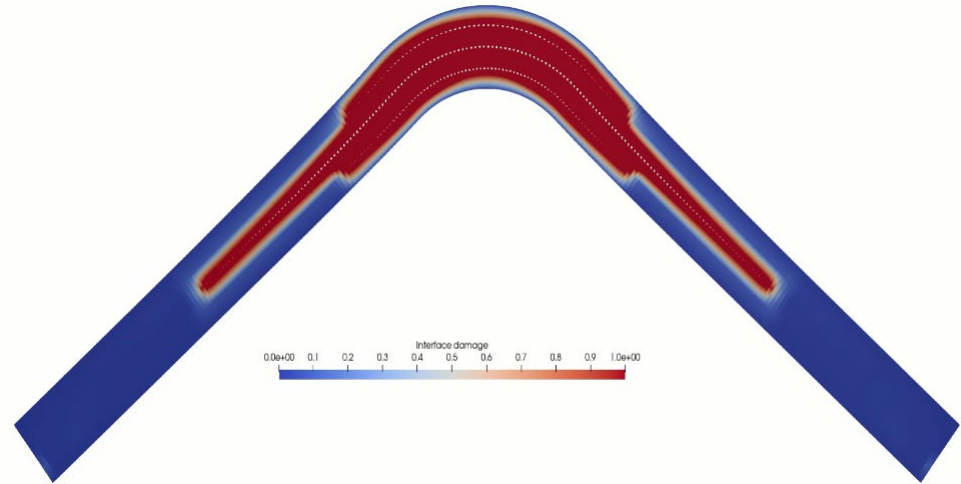


## Geometry:

$R_i = 5 \text{ mm}$ ,  $L_{\text{leg}} = 25.4 \text{ mm}$ ,  $t = 6.61 \text{ mm}$

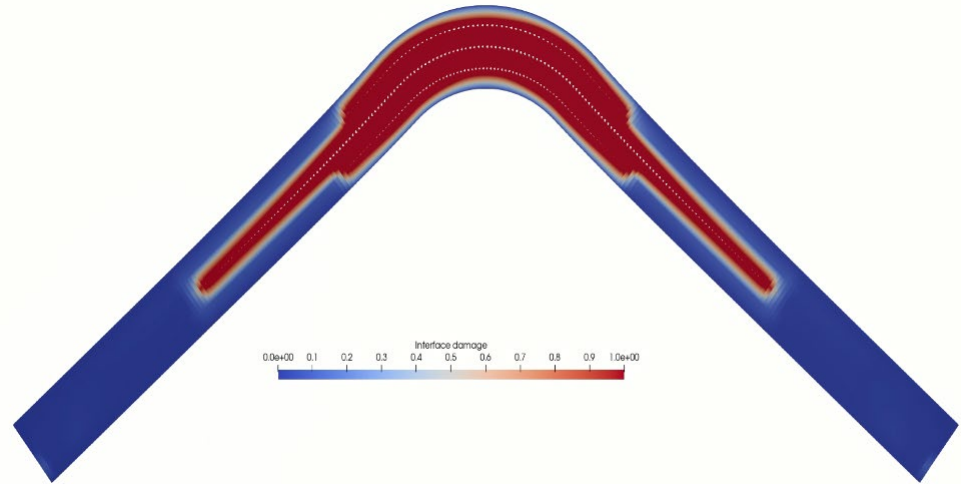
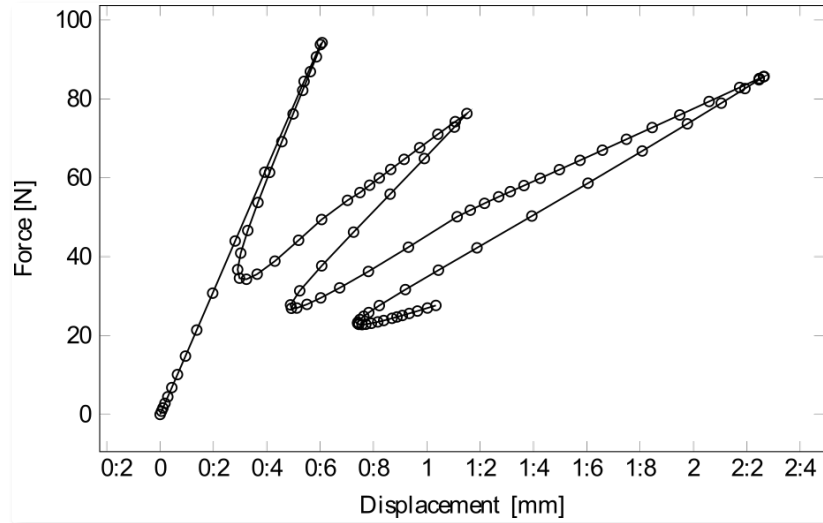
## Material properties:

$E_1$	141 GPa	$G_{12}$	5.8 GPa	$\nu_{12}$	0.3
$E_2$	11 GPa	$G_{13}$	5.8 GPa	$\nu_{13}$	0.3
$E_3$	11 GPa	$G_{23}$	3.9 GPa	$\nu_{23}$	0.4



# Example - “NASA specimen”

Elias Börjesson, Joris Remmers and MF: *Computational Mechanics 2022*



# Thank you!

## PhD students and post-docs:

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- Erik Svenning
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- Carolyn Oddy
- **Pierre Daniel**
- **Elias Börjesson**
- Ehsan Ghane
- **Jim Brouzoulis**
- Hana Zrida
- Mohsen Mirkhalaf

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- Magnus Ekh
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- Renaud Gutkin
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- **Pere Maimí**
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