

The Stress Invariant Simulator (SISi)

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An engineering toy to visualize stress invariants

(downloadable from the www.dynamore.de)

Crafting instructions

- Download the PDF-file (this file!)
- Print crafting sections on thick piece of paper
- Cut out where indicated
- Add four wooden sticks (approx. 15cm of length)
- Add some glue where necessary (engineers should find out the locations without further instructions from the pictures – all others contact their local distributor please)
- Have fun!



page 1:

Stress Invariant Simulator (SISi)

von Mises $\xi = -1$
 $\xi = 0$
 $\xi = 1$
 compression
 shear
 tension
 Tresca
 π -plane
 $\sigma_I = \sigma_{II} = \sigma_{III}$

Definition of stress invariants

$$I_1 = \sigma_I + \sigma_{II} + \sigma_{III} = \sigma_m = -3p = 3\sigma_m$$

$$J_2 = \frac{1}{2} s_y s_y \quad \text{where} \quad s_y = \sigma_y - \frac{I_1}{3} \delta_{ij}$$

$$\sigma_{vM} = \sqrt{3J_2}$$

$$\eta = \frac{\sigma_m}{\sigma_{vM}} = -\frac{p}{\sigma_{vM}} = \frac{I_1}{3\sigma_{vM}}$$

$$\xi = \frac{27}{2} \frac{J_3}{\sigma_{vM}^3} \quad \text{where} \quad J_3 = \det s$$

Haigh-Westergaard-coordinates

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DYNAMORE Stress Invariant Simulator (SISi)

DYNAMORE Stress Invariant Simulator – A. Haufe

DYNA
MORE

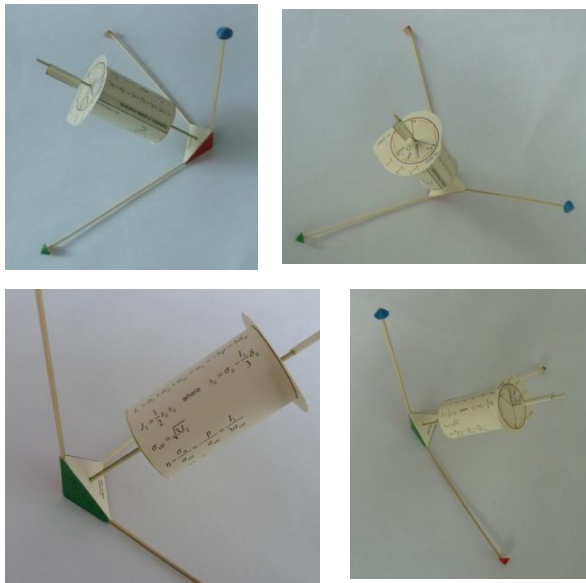
An engineering toy to visualize stress invariants

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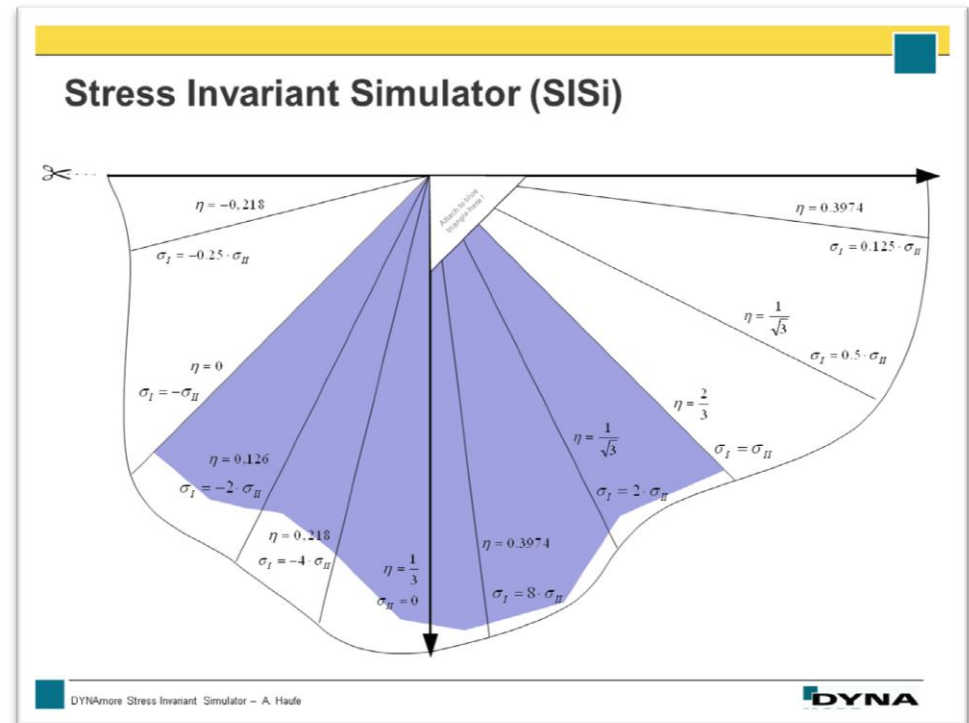
Crafting instructions

- Page 2 of the set may be added for further clarification of the triaxiality variable.

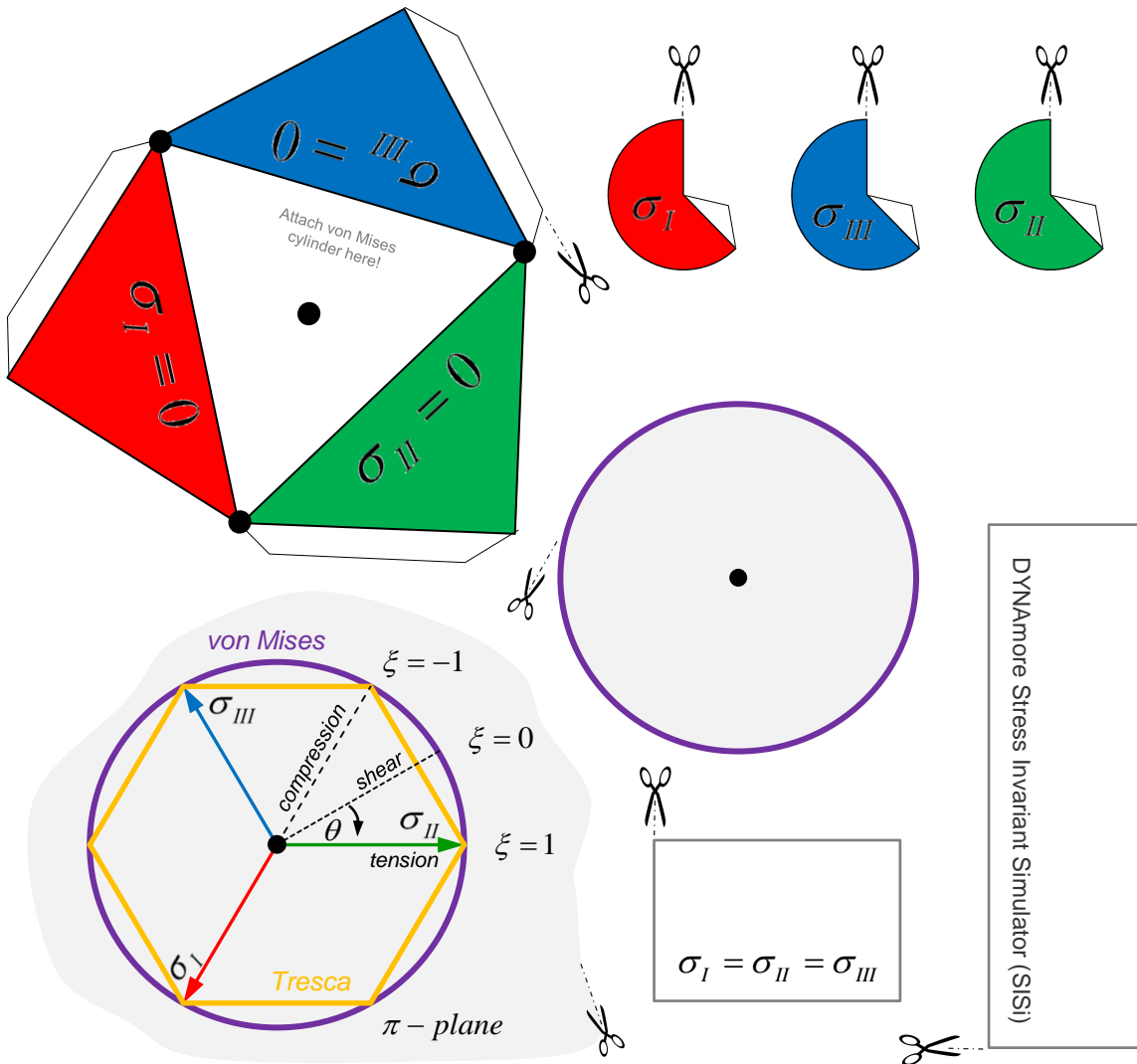
Final shape of toy



page 2:



Stress Invariant Simulator (SISi)



Definition of stress invariants

$$I_1 = \sigma_I + \sigma_{II} + \sigma_{III} = \sigma_{ii} = -3p = 3\sigma_m$$

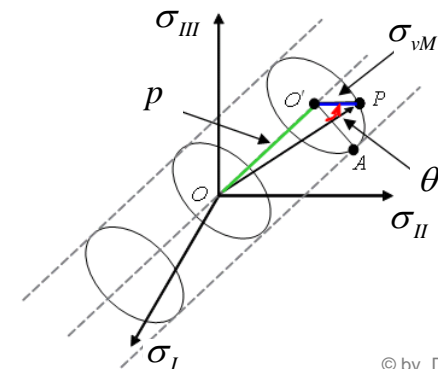
$$J_2 = \frac{1}{2} s_{ij} s_{ij} \quad \text{where} \quad s_{ij} = \sigma_{ij} - \frac{I_1}{3} \delta_{ij}$$

$$\sigma_{vM} = \sqrt{3J_2}$$

$$\eta = \frac{\sigma_m}{\sigma_{vM}} = -\frac{p}{\sigma_{vM}} = \frac{I_1}{3\sigma_{vM}}$$

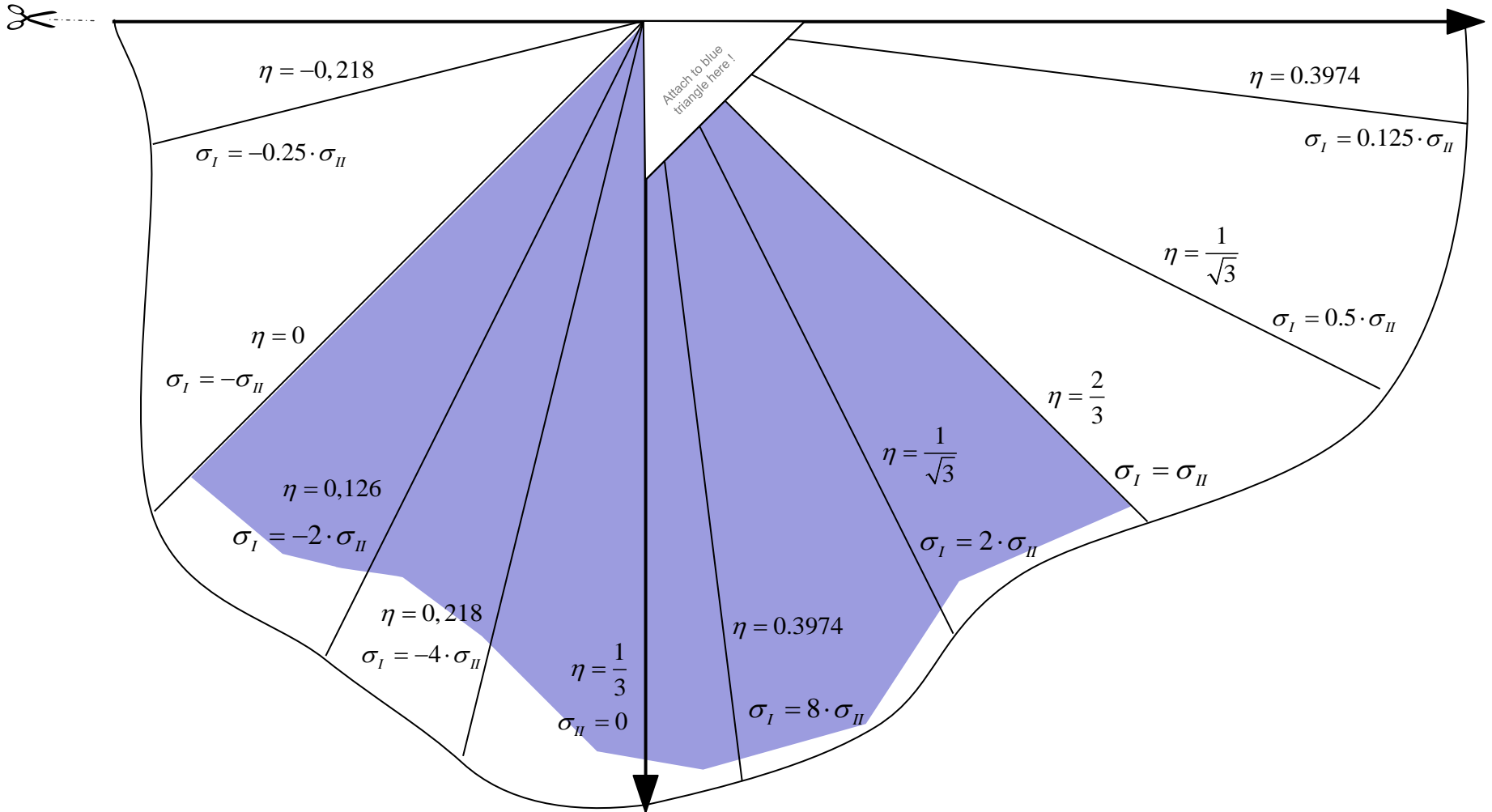
$$\xi = \frac{27}{2} \frac{J_3}{\sigma_{vM}^3} \quad \text{where} \quad J_3 = \det s$$

Haigh-Westergaard-coordinates



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